Chapter 3. Force and Gravity

Being in orbit is like being infatuated – you are constantly falling, but you aren't getting closer. (Modified 20 Sept 2005)

Gravity surprises

When orbiting the Earth, the head of an astronaut is "weightless." When he sneezes, it will snap back ...

exactly as much as it does when he is sitting on the Earth's surface

At an altitude of 100 km, you are virtually at the edge of space, since more than 99.999% of the Earth's atmosphere is below you. At this altitude, the force of gravity is less than at the Earth's surface. It is smaller by ...

about 1.6%.

The \$10 million "X Prize" was awarded last year to the first private company to send a rocket to an altitude of 100 km. Some think this is the beginning of private exploitation of space. But getting to 100 km takes less energy than it takes to get into orbit around the Earth. How much less?

thirty times less.

If the Sun suddenly turned into a black hole, but its mass didn't change (it is presently about 300,000 times the mass of the Earth), then the orbit of the Earth ...

wouldn't change.

Those facts surprise most people. That's because their understanding of gravity is confused by misunderstanding several important concepts, including weightlessness, orbits, and the behavior of gravity.

The Force of Gravity

Any two objects that have mass attract each other with a force we call gravity. You probably never noticed this for small objects, because the force is so weak. But the Earth has lots of mass, and so it exerts a big gravitational force on you. We call that force your weight. The fact that gravity is actually a force of attraction is not obvious. Prior to the work of Isaac Newton, it was assumed that gravity was simply the natural tendency of objects to move downward.

If you weigh 150 lb, and are sitting about 1 meter (3.3 feet) from another person of similar weight, then the gravitational force of attraction between the two of you is 10⁻⁷ lb. This seems small, but such forces can be measured; it is about the same as the weight of a flea.

You weigh less when you stand on the Moon, because the Moon doesn't put as big a force on you. If you weigh 150 lb on the Earth, you would weigh only 25 lb on the Moon. You haven't changed (you are made up of the same atoms), but the force exerted on you is different. Physicists like to say that your *mass* hasn't changed, only your weight. Think of mass as the amount of material, and weight as the force of attraction of gravity.

Mass is commonly measured in kilograms. If you put a kilogram of material on the surface of the Earth, the pull of gravity will be a force of 2.2 lbs. So a good definition of a kilogram is an amount of material that weighs 2.2 lbs when placed on the surface of the Earth. That number worth remembering, since kilograms are commonly used around the world.¹

Suppose you weigh 150 lb on the Earth. Then your mass is about 68 kg (i.e. it is 150/2.2). Go to the surface of Jupiter, and you will weigh nearly 400 lbs. On the surface of the Sun you will weigh about 2 tons, at least for the brief moment before you are fried to a crisp. But in all cases your mass will be 68 kg.

The equation that describes the pull of gravity between two objects was discovered by Isaac Newton. It says that the force of attraction is proportional to the mass – double the mass and the force doubles. The force also depends on the distance. It is an *inverse* square law. It is inverse because when the distance gets larger, the force gets smaller. It is a square law because if you triple the distance, the force decreases by nine; if you make the distance increase by 4, then the force goes down by 16, etc.

Newton's third law

Here is something that might surprise you: if you weigh 150 lb, not only is the Earth attracting you with a force of 150 lb, but you are attracting the Earth with a force of 150 lb too. This is an example of something called "Newton's third law" – if an object exerts a force on you, then you exert the same force back on it. In my mind, it is so fundamental that it should have been number one of Newton's laws. (Newton's first law is that an object in motion tends to stay in motion unless there is an outside force. Newton's second law, F = ma, is one we'll get to soon.)

But if you are so small, how can you exert such a large force on the Earth? The answer is that, even though you are small, your mass exerts a force on every piece of the Earth,

¹ A more accurate value is that there are 2.205 lb in a kilogram, and 0.4536 kg in a pound, but don't bother memorizing these more precise numbers.

simultaneously. When you add all those forces together, the sum is 150 lb. So you are pulling up on the Earth exactly as much as the Earth is pulling down on you.

Think of it in the following way. If you push on some else's hand, they feel your force. But you feel the force too. You push on them; they push back on you. The same thing works with gravity. The Earth pulls on you; you pull on the Earth.

The "weightless astronaut" paradox

Imagine an astronaut in orbit in a capsule 200 km (125 miles) above the surface of the Earth. What does he weigh? Because he is further away from the mass of the Earth, the force is slightly lower. From Newton's Law of Gravity, we can calculate that he is weighs 142 lb, i.e. he is 8 lb lighter.

But wait a minute – aren't orbiting astronauts weightless? Movies show them inside space ships floating around. How can they do that if they weigh almost as much as they do when they are on the surface of the Earth?

To understand the answer to this paradox, we have to think about what it means to be weightless. Suppose you are in an elevator, and the cable suddenly breaks. The elevator and you fall together. During those few seconds before you crash into the ground, you will feel weightless. You will float around inside the elevator. You will feel no force on your feet, and your shoulders will not feel the weight of your head. (Your head falls with your chest, at the same rate, so the muscles in your neck need exert no force to keep the head above the chest.) In those brief seconds you have the same "weightless" experience as the astronauts. All the time, of course, the Earth is pulling you rapidly towards it. You have weight, but you feel weightless. A movie made of you in the elevator would show you floating around, apparently without weight, while you and the elevator fell together. You would look just like the astronauts floating around in the Space Station.

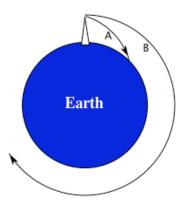
Now imagine that instead of falling, you and the elevator are shot together out of a gun, and fly 100 miles before hitting the ground. During that trip, you will again feel weightless. That's because you are in motion along with the elevator. You and it fly in the same arc.³ Your head and chest are both moving in that arc together; there is no force between them and your neck muscles can be completely relaxed. Your head will seem to have no weight. Prior to the space program, potential astronauts were flown in airplanes following such arcs in order to see how they responded to the sensation of weightlessness – and to get them used to it.

² There are rides at some amusement parks that allow you to fall for long distances and experience weightlessness, at least for a small number of seconds. We'll calculate how many seconds in a later section.

³ Your path is a geometric curve known as a parabola.

When you and the elevator are moving together under the force of gravity (either falling or shot in an arc) there seems to be no gravity. From that alone, you might think you were far out in space, far away from the gravity of any planet, star, or moon. From inside the elevator, you can't tell the difference.

Now imagine that at the top of a very tall tower (200 km high) is a large gun, pointing horizontally. We shoot the elevator and you horizontally. If we picked a low velocity (e.g. 2 km/sec) you and the elevator would curve towards the Earth, and you would crash into it, as in path *A* in the figure below. But instead we pick a high velocity: 8 km/sec. You and the elevator are shot from the gun, and you curve towards the Earth, but because of your high velocity, you miss the edge of the Earth, as in path *B*. You keep on curving downward, but you never hit. You are in orbit. The force of gravity makes the path of the elevator – let's call it a space capsule now – curve downwards. But if that curvature matches the curvature of the Earth, then it misses the surface, and stays at a constant height.⁴



capsule shot into space from a tower

This may seem preposterous, but it is reasonable to think of an astronaut in orbit around the Earth as being in a state of perpetual falling. That's why he feels weightless.

You can think of the Moon as doing the same thing. It is attracted to the Earth by gravity, but it has high sideways motion. Even though it is falling towards the Earth, is always misses.

The velocity for LEO (Low Earth Orbit)

To stay in a circular orbit just a few hundred miles above the surface, the velocity of the satellite must be about 8 km per second, which is about 18,000 miles per hour. (The actual value depends slightly on the altitude; we'll derive this number from a calculation

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⁴ If your velocity is not exactly horizontal, or if your velocity is a little low or high, then the orbit will not be a circle but an ellipse.

later in this chapter.) At this velocity, the satellite orbits the 24,000 mile circumference of the Earth in about 1.5 hours.

Remember this number: a satellite orbiting in a LEO (low Earth orbit) goes 8 km/sec and takes an hour and a half to go around the Earth.

If the astronaut wants to land, he does *not* point his rockets downward and fire his rockets away from the Earth; he fires his rockets towards the direction he is headed – in the forward direction! The force of the rocket exhaust slows down the satellite, so it is no longer going fast enough to miss the edge of the Earth. If he fired the rockets enough to stop the satellite completely, then it would simply fall straight downward. Gravity brings the satellite back to Earth. If the satellite moves faster than 8 km per second, it leaves the circular orbit and heads out into space. At about 11 km per second it will have sufficient velocity to reach the Moon and beyond. This velocity is called the escape velocity. We'll discuss this concept further later in this chapter.

Analogy with a rock and sling

There is another way to think about Earth satellites. Forget gravity for a moment. Imagine that you have a rock tied at the end of a string, and you are spinning it in a circle above your head. The string provides the force that keeps the rock from flying away, that keeps the rock in circular motion. If the string breaks, the rock flies off in a straight line. Gravity does the same thing for an Earth satellite: it provides the force that keeps the satellite in a circular orbit.

An old weapon called the "sling" is based on this principle. A rock is held by a leather strap, and spun in circles over the head. Arm motion helps it pick up circular speed. It is the strap that keeps the rock in circular motion. When the strap is released, the rock flies in a straight line towards its target. Such a sling was the weapon that, according to the Bible, David used to kill the giant Goliath.

In a similar manner, if we could suddenly "turn off" the force of gravity, the Moon would leave its circular orbit, and head off in a straight line. Likewise for all the satellites now in orbit around the Earth. And with the Sun's gravity turned off, the Earth would head out into space too, at its previous orbital speed of 30 km/sec (67,500 mph).

Geosynchronous satellites

Weather satellites and TV satellites have a very special orbit: they are "geosynchronous." This means that they stay above the same location of the Earth at all times. That means that the same weather satellite will be able to watch the development of a storm, or of a heat wave, continuously. It means that if you are receiving a signal for your TV, you never have to re-point the antenna. The satellite remains in the same direction above your house at all times.

How can this be, since satellites must orbit the Earth to avoid crashing back down? The answer is elegant: the satellites orbit the Earth at such a high altitude (where the gravity is weak) that they go at a low velocity, and take 24 hours for each orbit. Since the Earth rotates once in that period, they stay above the same location. Both are moving – your home with the TV dish, and the satellite – but their angle with respect to each other doesn't change.

Geosynchronous satellites orbit the Earth at the very high altitude of 22,000 miles. That distance is over 5 times the radius of the Earth. The force of gravity is an "inverse square" law. That means that if the distance is 5 times larger, then that factor makes the force 25 times smaller. Moreover, at the high altitude the distance to make a circular orbit is longer. These factors combine to make the time to circle the Earth equal to 24 hours, rather than the 1.5 hours of a LEO.

There is a catch. If the satellite is to stay in the same location in our sky relative to the ground, it must orbit above the equator. Can you see why that is true? A geosynchronous satellite moves in a circle around the center of the Earth. If the satellite is not in an equatorial orbit, then it will spend half of its orbit in the Northern Hemisphere, and half in the Southern. Only if it orbits above the equator can it stay precisely above the same Earth location at all times.

As a result, all geosynchronous satellites are right above the equator. If you look at them up in the sky, they all line up in a narrow arc. In fact, there is so little room left, that international treaties are required to divide up the space. (If satellites are too close to each other, their radio signals can interfere.)

If you are kidnapped, and don't know where you have been taken, try to spot a satellite dish. If the dish is pointing straight up, then you know you are on the Equator. If it is pointing horizontally, then you know you are at the North Pole.⁵

Spy satellites

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Spy satellites are satellites that carry telescopes to look down on the surface of the Earth and see what is going on. They were once used exclusively by the military, to try to see the secrets of adversaries, but now they are widely used by government and industry to look at everything from flooding and fires to the health of food crops.

The ideal spy satellite would stay above the same location all the time. But to do that, it must be geosynchronous, and that means that its altitude is 22000 miles. At those distances, even the best telescopes can't see things smaller than about 200 meters. (We'll derive that number when we discuss light.) That means that such a spy satellite could see

⁵ But be careful. Even at the equator, the satellite doesn't have to be overhead. The satellite could be above the Congo and you could be in Brazil. So you really have to determine the direction of north to make good use of the satellite dish information.

a football stadium, but couldn't tell if a game were being played. Such satellites are good enough to watch hurricanes and other weather phenomena, but are not useful for fine details, such as finding a particular terrorist.

Thus, to be useful, spy satellites must be much closer to the Earth. That means they must be in LEO (low earth orbit), no more than a few hundred miles above the surface. But if they are in LEO, then they are not geosynchronous. In LEO they zip around the 24,000 mile circumference of the Earth in 1.5 hours; that gives them a velocity relative to the surface of 16,000 miles per hour. At this velocity, they will be above a particular location (within \pm 100 miles of it) for only about 7.5 minutes. This is a very short time to spy. In fact, many countries that want to hide secret operations from the United States keep track of the positions of our spy satellites, and make sure their operations are covered over or hidden during the brief times that the spy satellite is close enough to take a photo.

LEO satellites cannot hover. If they lose their velocity, they fall to Earth. If you want to have continuous coverage of a particular location, you must use a circling airplane, balloon, or something else that can stay close to one location.

The military and intelligence agencies are developing quiet, high flying drones (airplanes without pilot) to do the most critical kind of spying. But these vehicles can be shot down more easily than a satellite.

GPS - A Medium Earth Orbit (MEO) satellite

One of the wonders of the last decade is the GPS satellite system. GPS stands for "Global Positioning System", and if you buy a small GPS receiver (cost under \$100), it will tell you your exact position on the Earth within a few meters. I've used such a receiver in the wilderness of Yosemite, in the souks of Fez, and in the deserts of Nevada. You can buy a car with a built-in GPS receiver that will automatically display a map on your dashboard showing precisely where you are. The military uses GPS to steer its smart bombs to land at just the location they want, within a few meters.

A GPS receiver picks up signals from several of the 24 GPS satellites currently orbiting the Earth. It is able to determine the distance to each satellite by measuring the time it took the signal to go from the satellite to the receiver. Once it knows the distance to three satellites, it can then calculate precisely where on Earth it is located.

To understand it does this, consider the following puzzle: A person is in a U.S. city. He is 800 miles from New York City, 900 miles from New Orleans, and 2200 miles from San Francisco. What city is he in?

Look on a map. There is only one city that has those distances, and that is Chicago. Knowing three distances uniquely locates the position. GPS works in a similar manner,

⁶ At 1600 miles per hour, it will go 200 miles in 1/8 of an hour = 7.5 minutes.

but instead of measuring distances to cities, it measures distances to satellites. And even though the satellites are moving, their locations when they broadcast their signals are known. They tell you're the computer in your GPS receiver where they are, so the GPS receiver can figure out where it is.

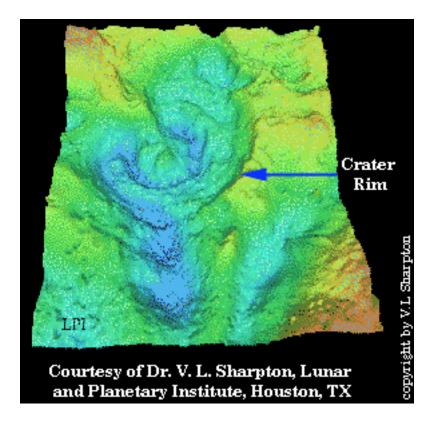
You might expect that the GPS satellites would be in geosynchronous orbits. But they are not, primarily because that such large distance would require that their radio transmitters have much more power to reach the Earth. They were not put in low orbit (LEO) because they would then often be hidden from your receiver by the horizon. (Each one would be in view for, typically, 7 minutes *if* it passed directly overhead.) So they were placed in a medium Earth orbit (MEO) about 12,000 miles high. They orbit the Earth every 12 hours.

Using gravity to search for oil

I said earlier that every object exerts a small gravitational force on every other object. Remarkably, measurement of such small forces has important practical applications. If you are standing over an oil field, the gravity you feel will be slightly less than if over solid rock, for the simple reason that oil is less dense than rock; it has less mass (per cubic kilometer), and so its gravity isn't as strong. Such small gravity changes can even be measured from airplanes flying above the ground. An instrument can make a "gravity map" that shows the density of the material under the ground. Maps of the strength of gravity, taken by flying airplanes, are commonly used by businesses to search for oil and other natural resources.

A more surprising use of such gravity measurements was to make a map of the buried crater on the Yucatan peninsula, the crater left behind when an asteroid killed the dinosaurs. The crater was filled in by sedimentary rock that was lighter than the original rock, so even though it is filled, it shows a gravity "anomaly," i.e. a difference from what you would get if the rock were uniform. An airplane flying back and forth over this region made sensitive measurements of the strength of gravity, and they produced the map shown below. In this map, the tall regions are regions in which the gravity was stronger than average, and the low regions were locations where the gravity was slightly weaker.

⁷ Optional footnote: The gravity of a spherical objects acts as if it is all coming from the center of the Earth. But this is true only if the sphere's mass is uniformly distributed. If there is an oil field, then you can mathematically think of that as a sum of a uniform Earth, and a little bit of "negative" mass that cancels out some of the gravity. If you are close to the oil field, you will sense the reduced gravity because this little bit of negative mass will not attract you as much as if it were denser rock.



The crater shows several concentric circles, with the largest over 100 km in diameter. The inner rings probably formed when the huge crater initially filled in as material from under the crater was forced upward, partially filling it.

manufacturing objects in a weightless environment

When the space program began, many people thought that there would be significant advantages to being in a weightless environment. In a satellite, things wouldn't sag under their own weight. It might be possible to make better (rounder) ball bearings, or to grow more perfect crystals (used in computers and other electronics) than can be done on the ground.

This promise has been largely unfulfilled. The additional cost of doing the work in a satellite has not turned out to be worth it. It costs about \$10,000 to launch a kilogram of anything into orbit. In the near future, commercial companies hope to reduce that price will come down to \$1,000 per kilogram. It's hard to make a profitable factory in space when it costs that much just to get there. There is no reason in principle why getting to space *must* be expensive; we'll show in a later section that the energy required is only 15 Cal per gram. Some time in the future, if travel to space becomes as cheap as an airplane ride, then the idea of factories in orbit may be more likely.

Gravity on the moon and asteroids

Our Moon has about 1/81 of the mass of the Earth. So you might think its gravity would be 81 times less. But the Moon's radius is 3.7 times smaller than that of the Earth. Remember that gravity is an inverse square law, so from the small radius you would expect the force to be $(3.7)^2 = 13.7$ times larger. If you combine these two effects, you get surface gravity 13.7/81 = 1/6 that on the Earth. And that is the value the astronauts found when they landed there. The gravity was so weak that they seem to bound around in slow motion. When they jumped, they went high, and when they came back down, the came down slowly.

What is the surface gravity of an asteroid that has a radius of 1 km? We can't say, since we don't know the mass. However, if you assume that the density is the same as for the Earth, then we can derive a simple result: the surface gravity is proportional to the radius. Since the radius of the Earth is 6378 km, this means that the surface gravity on an asteroid is 1/6378 of the value on the Earth. If you weigh 150 lb on Earth, you would weigh 150/6378 = 0.023 lb, or about a third of an ounce. That's about the weight of three pennies on the Earth.

As we'll show in a later section (on escape velocity) the person on the asteroid would have to be very careful, because his escape velocity would be very low. To jump into space from the Earth requires a velocity of 11 km/sec, but from the asteroid you would only require a velocity of 2 m/s. (The same jump speed would get you less than a foot high on the surface of the Earth.) You could easily launch yourself into space by jumping. This low escape velocity was a problem for a U.S. space probe called "NEAR" (stands for Near Earth Asteroid Rendezvous). If the satellite landed at a velocity of 2 m/s or more, then it might have bounced right back out into space.

Gravity in Science Fiction

One of the most common "errors" in Science Fiction movies is the implicit assumption that all planets in all solar systems have a gravity about equal to that on the Earth. There is no reason why that should be so. Pick a random planet, and you are just as likely to be a factor of 6 lighter (and bouncing around like astronauts on the Moon) or six times heavier and unable to move because of your limited strength. Imagine a person who weighs 150 lb on the Earth, trying to move on a planet where he weighs 900 lb.

mass of m = 1 kg on different planets will depend only on their radius R of that planet.

⁸ Optional footnote: That's because the mass of the asteroid M = density x volume. Call the density d. The volume of a sphere is $(4/3) \pi R^3$. So the gravity at the surface is F = $GMm/R^2 = G m (4/3 \pi R^3 d)/R^2 = G m (4/3 \pi d) R = constants x R$. So the weight of a

Falling to Earth

Let's now talk about everyday gravity, the gravity that you feel when you are near the surface of the Earth. When you jump off a diving board (or a bungee tower) gravity pulls you downwards. The force of gravity acts on all parts of your body, and makes them fall faster and faster. You accelerate, but in a very remarkable way: every second that you fall, you pick up an additional 9.8 meters per second of velocity. Put in the form of an equation, your velocity v after a time t is

$$v = g t$$

where the constant g = 9.8 is usually called the acceleration of gravity.

By *acceleration* we mean the rate at which your velocity changes. For gravity, the acceleration is constant. After one second, your velocity is 9.8 meters/sec. After two seconds, it is 19.6 m/s. After three seconds, 29.4 m/s. After 4 seconds, 39.2 m/s. Every second you pick up an additional 9.8 m/s.

Here is a useful conversion factor:

$$1 \text{ m/s} = 2.24 \text{ mph}$$

After falling for 4 seconds, the velocity was 39.2 m/s. To convert this to mph, just multiply by 2.24. So the velocity after 4 seconds is $39.2 \times 2.24 = 88$ miles per hour. That may give you a better sense of how fast you're moving. How far will you fall in this time? The equation can be derived using calculus.⁹ The answer is:

$$D = \frac{1}{2}gt^2$$

You are not required to memorize this equation; I show it so you can see how we do these calculations. If we put in t = 4 seconds, this gives 10 D = 78 meters = 257 feet. That's how far you'll fall in 4 seconds.

We can also use the equations backwards to see how long it takes to fall a certain distance. In 1939, when King Kong fell off the Empire State Building, it was 330 meters high. ¹¹ So how long should it have taken him to fall from the top to the bottom? Take our equation for *D* and solve for *t*. This gives:

⁹ Optional footnote: According to calculus, the distance $D = \int v dt = \int g t dt = g \int t dt = (1/2) g t^2$.

 $^{^{10}}$ D = (1/2) 9.8 $(4)^2$ = 78 meters

¹¹ In 1939 the Empire State Building was only 6 years old, and did not yet have the 250 foot TV antenna on its top.

$$t = \sqrt{\frac{2D}{g}}$$

Put in D = 330, g = 9.8, to get that t = 8.2 seconds. Watch the movie (the 1939 version) and see if this matches what is in the movie.

How fast was Kong moving when he hit the ground? We just calculated that t = 8.2 seconds. We can put that into our velocity equation to get

$$v = g t = 9.8 \times 8.2 = 80 \text{ m/s}$$

Remember that 1 m/s is 2.24 mph. That means that Kong was falling at $2.24 \times 80 = 180$ miles per hour when he hit. No wonder he was killed.

Dropping food, terminal velocity, and parachutes

In 2002, during the U.S. war in Afghanistan, food was dropped out of airplanes to feed the Afghan people. The food was dropped from an altitude of 3000 meters (about 10,000 ft). How fast was it going when it hit the ground?

Let's use the equations to figure this out. The time it took to fall was:

$$t = \sqrt{\frac{2D}{g}} = \sqrt{\frac{2x300}{9.8}} = 24.7 \text{ seconds}$$

and so its velocity would have been

$$v = g t = 9.8 \text{ x } 24.7 = 2425 \text{ m/s}$$

= 5335 miles per hour

That is incredibly fast. The speed of sound is only 330 meters per second, so according to these equations it was going 7.3 times the speed of sound, also called *Mach 7.3*.

Suppose the object slows down by friction with the air, and that all its energy goes into heating the object. (We'll ignore for a moment the heating of the air.) In Chapter 2 we showed that the temperature it reaches at Mach number M will be M^2 x 300 K. So from friction with the air, the food should have heated up to 7.3^2 x 300 K = 16,000 K, more than twice as hot as the surface of the Sun! It all should have been vaporized. Clearly that didn't happen to the food dropped on Afghanistan. Our calculation was wrong. But what did we do wrong?

We made the mistake of neglecting the force of air as the packages were dropped. Every time the package hits a molecule of air, it transfers some of its energy. The force F of air depends on the area A of the package (more area means it hits more air molecules).

That's not surprising. But more interesting is the fact that the force depends on the square of the velocity. Double your velocity, and the force goes up four times; go 3 times faster, and your force increase by 9. This means that air resistance becomes extremely important at high velocities. This fact is the key to understanding not only dropped food, but also parachutes, space capsule reentry, and automobile gasoline efficiency.

As the object falls faster and faster, the force of air resistance gets greater and greater. Gravity is pulling down, but the air is pushing up. The force of the air resists the gravity; it opposes it. If the object keeps on accelerating, eventually the force of air will match the weight of the object. When that happens, gravity and air resistance are balanced. The object doesn't stop moving, but it stops accelerating, that is, it no longer gains additional velocity. When this happens we say the falling object has reached *terminal velocity*.

For the food dropped over Afghanistan, the terminal velocity was about 9 mph. For a falling person it is typically 70-100 mph. That's fast, but people have survived falls from great heights into water. (Try to imagine this next time you are going in a car or train at 74 mph.) If a falling person spreads out his arms and legs (like sky divers) that increases the effective area, and the person will fall even slower. A person using a parachute is not much heavier, but the parachute area A is large, so the terminal velocity is only about 15 mph. For King Kong (about the same area as a parachute, but much heavier) the terminal velocity was several hundred mph; he hit the ground without ever reaching terminal velocity.

It is interesting to think about why objects that have fallen a long distance fall at the terminal velocity. If the falling object went any faster, the upward force (from the air) would be greater than the weight, and that net force would slow the fall. If the packet fell any slower than this terminal velocity, then the downward pull of gravity would be stronger than the upward force of air resistance, and the packet would fall faster. Only when the velocity is the terminal velocity does it not accelerate (go faster or slower).

Here are the terminal velocities for some interesting objects. 12

food packet: 4 meters/sec = 9 miles per hour

person in free fall: 33 meters/sec = 74 mph person with parachute (larger area): 6 meters/sec = 13 mph

¹² Optional footnote: The equation for terminal velocity is $v = \sqrt{\frac{2mg}{A\rho}}$. So, for example,

if a food packet has a mass of 0.1 kg, an area of 0.1 square meters, and we put in g = 9.8 and density $\rho = 1.25 \text{ kg/m}^2$, this gives v = 4 m/sec = 9 mph.

Automobile fuel efficiency

A moving car feels the force of air on its front, and that tends to slow the car down. To keep going at the same velocity, the engine must make up the lost energy. We'll show that much of the gasoline used by the car is to overcome the force of this air resistance. That is an important fact to know. At a velocity of 30 m/s = 67 mph, the force of air on the front of the car will be about 500 lb!

To keep the car from being slowed down by this force, the engine must exert an equal and opposite force. That takes a lot of gasoline. At these high velocities, more than 50% of the gasoline is used to overcome this air resistance. As a result, car designers have worked hard to "streamline" the shape of automobiles. If, instead of hitting the air with a flat surface (as in the old autos from the 1920s) you tilt the front surface, then the force can be much less, since the molecules can bounce off obliquely instead of hitting the front and bouncing straight back. In such a car, the force can be as low as 100 lb.

Many truck drivers are in business for themselves, and they have to pay for the extra gasoline used to overcome air resistance. Maybe you've noticed the smooth curves that some truck drivers have added to the cabs of their trucks to do the same thing. Reducing the force can save substantial money on gasoline.



Figure: Aerodynamic design for a truck cab

The top of the cab has had a contoured shape added to it to make the air bounce off smoothly, at an angle, instead of hitting the flat face of the truck head on. (The added shape is called "fairing.") This is shape change is sometimes called "aerodynamic smoothing" and it saves gasoline. It makes the effective value of "A", the area in the air resistance equation, smaller.

Note also that at half that speed (i.e. if v = 15 m/s = 33 mph) the force is four times less. That means that you use 4 times less gasoline to overcome air resistance. So you save even more gasoline by driving slower.

Force and Acceleration

If you push on an object, and there is no friction to hold it back, then it gains velocity. If you push twice as hard, it gains twice as much velocity. The acceleration is proportional to the force. But it also depends on the mass of the object. If the object has twice the mass, it needs twice the force to get it moving. These two facts are summarized the following equation:

Newton's Second Law:

F = k m a

In this equation, m is the mass (in kg), a is the acceleration (in m/s per second), and k is a constant. For the force F to be in pounds, k is 0.224. If you prefer the force in the physicist units called $Newtons^{13}$, then k = 1. That's why Newton's Second Law is usually written (in physics texts) as F = m a.

This equation tells you how much things speed up – or slow down -- when you apply a force.

This is Newton's Second Law. You may recall that Newton's *First* Law states that unless an object has an outside force on it, it will tend to keep its motion unchanged. But that is just a special case of the Second Law, since if F = 0, there is no acceleration, and that means no change in velocity. Nobody would ever teach the First Law these days if not for the fact that students sometimes wonder what came before the Second Law.

g

In this book, accelerations are typically measured in m/s per second. For automobiles, we frequently measure acceleration in miles per hour every second, sometimes written as mph/sec. For example, if a car salesman tells you that a car will "go from zero to sixty in ten seconds" what he is really telling you is the acceleration: 60 mph in 10 seconds. That is the same as 6 mph every second = 6 mph/s.

Optional footnote: Most physics texts measure force in *Newtons*, so the equation you'll see there is F = ma. Some physics texts will take this equation as the definition of mass. In that case, Newton's Second Law can be stated as follows: "the mass of an accelerating object is approximately constant." As we will see in the chapter on Relativity, at extremely high velocities, this law breaks down; mass increases with velocity.

Another very useful unit for acceleration, used in the military and by NASA, is the "g", pronounced "gee." One g is 9.8 meters/sec every second, i.e. it is the acceleration of gravity. Suppose an automobile accelerated at one g. How fast would it be going in 10 seconds? The answer is found from our velocity equation by setting a = 9.8:

$$v = a t$$

$$= 9.8 \times 10$$

$$= 98 \text{ meters/sec}$$

We can convert this to miles per hour by multiplying by 2.24 to get 219 mph. Obviously cars don't go this fast. That's because they don't accelerate at one g, but only at a small fraction of a g.

According to a NASA web site, when the Space Shuttle is launched, the acceleration reaches a maximum of 3 g. This is usually pronounced as "three gees." You've probably heard this term used in news programs and in movies. A pilot in an F-18 fighter plane sometimes accelerates as much as 10 g, i.e. "ten gees." Ten g would be $10 \times 9.8 = 98$ meters/sec every second. Weightlessness is often described as "zero g." That's when there is no gravity, or (if you are in space) no acceleration.

The g-rule

There is a very good reason to think of acceleration in terms of gs: it enables you to solve important physics problems in your head. Suppose I told you that I am going to accelerate you in the a horizontal direction by 10 gs. How much force will that take? The answer is simple: 10 times your weight! When astronauts are accelerated by 3 gs, the force on them to do this must be 3 times their weight. I call this the "g-rule": the force to accelerate an object is equal to the number of gs times the weight

To get the number of gs, just calculate the acceleration in m/s per second, and divide by 9.8. So, for example, we write that an acceleration of a = 19.6 m/s per second = 2 g. This is an acceleration of two gs. To accelerate something to 2 gs takes a force equal to twice the weight of that something.

Shooting an astronaut into space: the rail gun

To go into orbit around the Earth, a satellite must have a velocity of 8 km/sec. Why not give it this velocity in a gun? Could we literally "shoot" an astronaut into space?

The answer is: you might be able to do this, but the astronaut would be killed by the force required to accelerate him. Let's assume we have a very long gun, an entire kilometer

long. If we calculate the required acceleration to do this 14 , we get a = 408 g, i.e. the acceleration is 408 times the acceleration of gravity.

That's a lot of gs. Remember the g-rule: the force that it will take to accelerate you this fast will be 408 times your weight. So if you weigh 150 lb, the force that must be applied to you is $408 \times 150 = 60,000 \text{ lb} = 30 \text{ tons}$. That is enough to crush your bones.

Suppose we want to experience no more than 3 gs – that what the Space Shuttle does. How long would the gun have to be to get you going at v = 8 km/s? The gun would have to be 1000 km long! That is, of course, ridiculously impractical.

Of course, acceleration over such long distances is not impractical – it's what the Space Shuttle does. It takes off, accelerates at 3 gs, and it must go over 1000 km to reach orbital speed. So it is like a very long gun, but without a barrel. It actually takes the Space Shuttle further than 1000 km since 3 gs is only the peak acceleration; for most of the flight, the acceleration is less.

Acceleration during airplane take off

The take-off speed for a commercial airplane is about 160 mph. What acceleration is needed to achieve this speed in a 1 km runway? Let me make that question a little more personal. You are sitting in such an airplane. In a few seconds, you will be at the other end of the runway, and you will be moving (along with the airplane) at 160 mph. What force does the seat have to apply to your back to accelerate you?

We show in the footnote¹⁵ that this requires the airplane to accelerate at 2.6 m/s per second. We can convert this number to g units by dividing by 9.8, to get that the acceleration is 2.6/9.8 = 0.27 g. So the force that the airplane must push on you to get you going that fast is 0.27 times your weight, i.e. about a quarter of your weight. If you weigh 150 lb, then the push you feel on your back will be about 41 lbs. Think of this next time you are on an airplane taking off. Does this number feel about right?

Circular acceleration

Physicists like to define velocity as having magnitude and direction. If your velocity changes, we call it acceleration. But suppose you only change your direction and not the

 $^{^{14}}$ Optional calculation: The distance D = 8 km = 8000 meters, and the velocity v = 8 km/sec = 8000 m/sec. The relationship between distance, acceleration, and velocity is v² = 2 a D. Put in v and D, and solving for a gives a = 4000 m/s per sec. To covert this to gees, divide by 9.8 to get a = 4000/9.8 = 408 g.

¹⁵ I convert 160 mph to meters/sec by dividing by 2.2. So the airplane final speed is 160/2.2 = 73 meters/sec. I use the same equation I used in the prior footnote: $v^2 = 2$ a D. Put in v = 73, and D = 1000, for a = $v^2/(2 \text{ D}) = 73^2/2000 = 2.6$ m/s every second.

actual number of m/s? We still call that acceleration. ¹⁶ The reason we do that is that many of the equations we've been using still work.

The most important example of this kind of acceleration is when you go in a circle. If the magnitude of your speed is v, and this doesn't change (you keep going the same number of m/s or mph), and the circle has radius R, then we say that the circular acceleration is

$$a = v^2/R$$

This kind of acceleration is very important for the fighter pilot who is trying to change his direction rapidly. For example, if he is moving at velocity of 1000 mph, and is turning in a circle of radius R = 2 km, then his acceleration turns out to be 10 g. That's about as much as a fighter pilot can tolerate. We do the calculation in an optional footnote.¹⁷

The problem with accelerating more than 10 gs is that a human's blood pressure is not great enough to keep the blood in the brain, and that causes the pilot to faint. Even specially chosen and physically fit fighter pilots cannot take more than 10 g.

Fighter pilots and astronauts are usually tested and trained in a spinning cylinder, rotated fast enough for them to experience 10 g circular acceleration.

High g, from circular acceleration, is also a method used to separate the components of uranium for making a nuclear weapon. Such a device is called a **centrifuge**. The heavier parts of the uranium feel a greater force, and they are pulled more strongly towards the outer parts of the spinning cylinder. Such centrifuges are much in the news. In 2004, Libya disclosed the fact that it had purchased large centrifuge plants for the production of nuclear weapons material. Parts of such centrifuges have been found hidden in Iraq. We'll talk more about these centrifuges when we get to the chapter on nuclear weapons.

gravity in space - according to science fiction

the text.

Science fiction movies sometimes show a large rotating satellite. There is then "artificial gravity" from the rotation, and astronauts can walk around on the outside. This actually makes sense. The astronauts will feel a force on their feet (which point towards the

¹⁶ Optional: For people who have studied vectors: velocity is defined in physics as a vector. If the velocity at time t_1 is $\mathbf{v_1}$, and at t_2 is $\mathbf{v_2}$, then the acceleration vector is defined as $(\mathbf{v_2}-\mathbf{v_1})/(t_2-t_1)$. Even if the velocity is only changing in direction, the difference vector $(\mathbf{v_2}-\mathbf{v_1})$ is not zero. For circular motion, its magnitude is given by the equation in

optional calculation: acceleration of fighter pilot. First we convert these to metric units. We convert mph to m/s by dividing by 2.24, giving v = 1000/2.24 = 446 m/s. We also convert R to meters: R = 2000 meters. Plugging these in gives: $a = (446)^2/2000 = 100$ m/s per sec. We convert this to g's by dividing by 9.8 to get $a = 100/9.8 \approx 10$ g

outside) that will appear to them indistinguishable from gravity. Such a satellite is shown in the class movie 2001 - A Space Odyssey. We'll show in an optional footnote¹⁸ that the edge of a 200 meter-radius satellite must be moving at about 44 meters/sec. That means it will rotate once every 40 seconds.

artificial gravity in space - without circular motion

Many science fiction movies show space voyagers in the space ships walking around as if on the Earth. Is that nonsense? Where does that gravity come from?

I can make sense out of it. I just assume that the space ships are not moving at constant speed. If the ship engine accelerates the ship by a = 9.8 meters per second, then the ship will put a force on any astronauts inside to accelerate them too. A person of mass m will feel a force F = ma. But since the engines have set $a \approx g$, the force on the astronaut will be F = mg. That is exactly his Earth weight. If he places his feet on the backside of the ship (opposite in direction to the path the ship is taking) then he will feel like he is standing on Earth. In fact, he can't even tell the difference; the acceleration serves as a "virtual" gravity.¹⁹

Here is an interesting number: the distance the ship would travel in a year if it had constant acceleration of g. I do the calculation in an optional footnote. The answer is 5×10^{15} meters, which is about a half light year (the distance that light travels in a year). The distance to the nearest star (not counting the sun) is about 4 light years.

Escape to space

Suppose you want to completely leave the Earth. Just going into orbit isn't enough; you want to get far away, maybe to take a trip to the Moon, Mars, or a distant star. That takes more energy than just going into orbit. How much more? The answer is surprisingly

¹⁸ If the satellite has radius R and is rotating with a rim velocity v, then the force on the astronauts fee will be $F = m \, a$. If we use the formula for circular acceleration, $a = v^2/R$, then this becomes: $F = m \, v^2 R$. To make this equal to the astronaut's weight, we set F = mg. Solving for v, we get $v = \operatorname{sqrt}(g \, R)$. For a satellite with a radius of R = 200 meters, the rim velocity must be $v = \operatorname{sqrt}(9.8 \times 200) = 31$ meters per second.

¹⁹ Movies sometimes show the virtual gravity as being off to the side. This could be accomplished by having special sideways thrusters to accomplish this. Every hour or so the thrusters could rotate the ship around so it doesn't wind up going too far sideways.

optional calculation: The distance that you travel at acceleration g is given by our distance equation: $D = (1/2) g t^2$. We put in g = 9.8. For standard physics units ("MKS" meaning meters kilograms and seconds), we need to have t in seconds. We can calculate the number of seconds in a year as follows: 1 year = 365 days = 365 x 24 hours = 365 x 24 x 60 minutes = 365 x 24 x 60 x 60 seconds = 3.16×10^7 seconds. Plugging in this value we finally get $D = (1/2) \times 9.8 \times (3.16 \times 10^7)^2 = 5 \times 10^{15}$ meters. One light year is the speed of light (3 x 10⁸ m/s) times the number of seconds in a year (which we just showed was 3.16×10^7 seconds). That gives 9.5×10^{15} meters.

simple: exactly twice as much. You can get that much kinetic energy by going 1.414 times faster than orbital speed. (That's because energy depends on the square of the velocity, and $1.414^2 = 2$.) Since orbital velocity is 8 km/sec, that means that escape velocity is 8 \times 1.414 \times 11 km/sec.

These are good numbers to know:

orbital velocity: 8 km/sec for low earth orbit (LEO)

escape velocity: 11 km/sec for the Moon or beyond (to infinity!)

It is very interesting that the escape velocity does not depend on the mass. More massive objects do require more energy to escape, but at the same velocity, more massive objects already have more energy! Remember $E = (1/2) m v^2$. At escape velocity, an object with 2 kg mass has twice the energy as an object of 1 kg.

Black holes²¹

Big planets have high escape velocities. For Jupiter, it is 61 km/sec. For the sun it is 617 km/sec. Are there any objects for which the escape velocity is higher than the speed of light, 3×10^5 km/s = 3×10^8 m/s? The surprising answer is *yes*. We call such objects black holes. They get their name from the fact that even light cannot escape, so we can never see their surface; they are black. We'll show in Chapter 11 that no ordinary object (made out of mass as we know it) can go faster than the speed of light. That means that nothing could escape a black hole.

If the black hole is invisible, how do we know it's there? The answer is that even though it can't be seen, we can see the effects of its very strong gravity. When there is nothing visible, but the gravity is so strong that we know there must be something of great mass present, then we deduce it must be is a black hole.

To be a black hole, you have to do one of two things: either have a lot of mass, or pack a moderate amount of mass into a very small radius. Several black holes are known to exist; even though we can't see them (no light leaves the surface) we know that they are there because of their strong gravitational force they exert. The known black holes are all as massive as a star – or greater. But if you were to take the mass of the Earth and pack it inside a golf ball (in principle this is possible), then it would be a black hole. The mass would be the same, but the radius would be so small that the gravitational force on the surface of the golf ball would be enormous.

²¹ Why is the physics of black holes included in a text titled "Physics for future Presidents"? Is there any practical use for this knowledge? The answer is: no, not really. It is included, as are a few other things in this book, just because most people have heard about them and are curious. But you never know. Knowing the size of a black hole once won the author of this book a free guide to Paris. Outside of Shakespeare Books on the west bank of the Seine was a sign offering this prize if anyone could answer the question, "What size would the Earth have to be for it to be a black hole."

The sun is more massive, so you don't have to pack it so tightly. It would be a black hole if you packet it inside a sphere with radius 2 miles.

There are several black holes that were created, we believe, when the inner part of a star collapsed from its own weight into a very small radius. The object in the sky known as Cygnus X-1 is thought to be a black hole from such a collapse. If you have spare time, look up Cygnus X-1 on the web and see what you find.

Many people now believe that large black holes exists at the center of the large collections of billions of stars known as galaxies, such as the Milky Way galaxy. We presume these were created when the galaxy formed, but we know almost none of the details about how this happened.

Even more remarkably, the Universe itself may be a black hole. That's because the black hole radius for the Universe is about 15 billion light years, and that is approximately the size of the observable Universe. In other words, the Universe appears to satisfy the black hole equation. We'll discuss this further in Chapter 12. But you probably won't be surprised at one inescapable conclusion that follows²²: we can never escape from the Universe.

Momentum - return to Newton's third law

If you shoot a powerful rifle, then the rifle puts a large force on the bullet sending it forward. But the bullet puts a backward force on the rifle, and that is what causes the "kick." The rifle can suddenly go backwards so rapidly that it can hurt your shoulder. If you don't have your feet firmly planted on the ground, you will be thrown backwards.

Recall that we discussed Newton's third law earlier – the fact that if you push on something, it pushes back on you. Newton stated this as "for every action there is an equal and opposite reaction." But we no longer use this old terminology of "action" and "reaction." Instead we say that if you push on an object (such as a bullet), then the bullet also pushes back on you for exactly the same amount of time. Of course, the bullet is lighter, so it is accelerated much more than you are.

Based on the fact that the bullet pushes on the rifle for the same time that the rifle pushes on the bullet, we can derive²³ an extremely important equation, sometimes called the

²² pun intended

The derivation is based on calculus. If an object is at rest, and it experiences a force F for a time t, then its velocity $v = \int a \, dt = \int (F/m) \, dt$. Write this as $m \, v = \int F \, dt$. If there are two objects, and the forces are equal and opposite, and the time is exactly the same, then $\int F \, dt$ is equal and opposite for the two objects, and that means that the quantity m v must also be equal and opposite for the two objects.

conservation of momentum. For the rifle (subscripts R) and the bullet (subscripts B), the equations are:

$$m_B v_B = m_R v_R$$

The equation for the rifle recoil is simple: the mass of the bullet, times its velocity, is the same as the mass of the gun times its recoil velocity. Of course, the velocities are opposite; this is sometimes indicated by putting a minus sign in front of one of the velocities. (I didn't do that here.) When the gun is stopped by your shoulder, then you recoil too – but less, because you have more mass.

The product m v is called the "momentum." One of the most useful laws of physics is called "the conservation of momentum." Before the rifle was fired, the bullet and gun were at rest; they had no momentum. After the rifle fired, the bullet and the rifle were moving in opposite directions, with exactly opposite momenta (the plural of momentum), so the total momentum was still zero.

Here's another way to say that: when you fire a gun, the bullet gets momentum. You and the rifle you are holding get an equal and opposite momentum. If you are braced on the ground, then it is the Earth that recoils with that momentum. Because the Earth has large mass, its recoil velocity is tiny, and difficult to measure.

If the objects are in motion prior to the force acting, then what happens is that the *changes* in momentum must be equal and opposite. Let's apply that to the comet that crashed into the Earth and killed the dinosaurs. To make the calculations easy, assume that before the collision the comet with mass m_C was moving at $v_C = 30$ km per second (a typical velocity for objects moving around the Sun). Assume the Earth was at rest. After the collision, the total momentum would be the same. The Earth would have mass m_E (that now included the mass of the comet) and have velocity v_E . So we can write

$$m_C v_C = m_E v_E$$

Solving for v_E we get

$$v_E = m_C v_C / m_E$$

The mass of the comet is about 10^{19} kg.²⁴ Everything else is known, so we can plug into this equation and get the v_E , the velocity of recoil of the Earth:

$$v_E = (10^{19})(30000)/(6x10^{24})$$

= 0.05 meters per second
= 5 cm per second
= 2 inches per second

-

²⁴ A comet with a radius $R_C = 100 \text{ km} = 10^5 \text{ meters}$, has a volume of $V_C = 4/3 \pi R_C^3$ (for a sphere) = 4.2×10^{15} cubic meters. Assuming that the comet is made mostly of rock and ice, the density is probably about 2500 kg per cubic meter, so the mass is 2500 x 4.2×10^{15} = 10^{19} kg.

That's not much of a recoil, at least when compared to the usual velocity of the Earth, which is 30 km/sec = 30,000 meters/sec. So the Earth was hardly deflected. It's orbit changed, but only by a tiny amount.

Let me estimate how much a truck recoils when it is hit by a mosquito. Assume (from the point of view of the truck, the mosquito (mass of 2.6 milligrams) is moving at 60 mph = 27 meters per second. Assume the truck weighs 5 metric tons = 5000 kg. (Hint: use the same equation, except let the 2.6 milligram mosquito represent the comet. Don't forget to convert everything to the same units: kilograms and meters.)

Although the conservation of momentum is one of the most important laws of physics, it is violated in many action movies. For example, if the hero in the Matrix punches the villain, and the villain goes flying across the room, then the hero should go flying backwards (unless he is braced on something big and massive). Likewise, small bullets, when they hit a person, seem able to impart very large velocities to the person that they hit, so the person goes flying backwards.²⁵

Rockets

Imagine trying to get into space by pointing a gun downward and firing bullets so rapidly that the recoil pushes you upward. Sound ridiculous? Yet that is exactly how rockets work.

Rockets fly by pushing burned fuel downward. If the fuel has mass m_F and is pushed down with a velocity v_F , then the rocket (which has mass m_R) will gain an extra upward velocity v_R given by the same kind of equation we used for the rifle:

$$v_R = v_F m_F / m_R$$

Compare this to the rifle equation, and to the comet/Earth collision equation.

Because the rocket weighs so much more than the fuel which is expelled every second (i.e. m_F/m_R is tiny), the amount of velocity gained by the rocket is much less than the fuel velocity. As a consequence, rockets are a very inefficient way to gain velocity. We use them to go into space only because in space there is nothing to push against except expelled fuel. Another way to think of this is as follows: rockets are inefficient because so much of the energy goes into the kinetic energy and heat of the expelled fuel, rather than in the kinetic energy of the rocket.

The equation above gives the velocity *change* when a small amount of fuel is burned and expelled. To get the total velocity given the rocket, you have to add up a large number of

²⁵ As a fan of this movie, I explain to myself that according to the script, "reality" is just a computer program called *the matrix*. Therefore I can assume that whoever programmed *the matrix* simply forgot to put in conservation of momentum. (Or, as James Gill suggests, Neo and the others altered the program to violate the laws of physics.)

such expulsions. Meanwhile, the mass of the rocket (which is carrying the unused fuel) is changing as fuel is used up. A typical result is that the rocket must carry huge amounts of fuel. The mass of fuel used is typically 25 to 50 times larger than the payload put into orbit.

For a long time, this huge fuel to payload ratio led people to believe that rockets into space were impossible; after all, how could you even hold the fuel if it weighed 24 times as much as the rocket? The problem was solved by using rockets with multiple stages, so that the heavy containers that held the initial fuel never had to be accelerated to the final orbital velocity. For example, for the space shuttle, the final payload (including orbiter weight) is 68,000 kg = 68 tons, and the amount boosters plus fuel weighs²⁶ 1931 tons, a factor of 28 times larger. Of course, the booster never gets into orbit, only the much smaller shuttle.

balloons, rockets, and astronaut sneezes

When you inflate a balloon, and then release the end, the balloon goes whizzing around the room, driven by the air being pushed out the end. What is happening is nearly identical to the way a rocket flies. Before you release the balloon opening, the balloon and the air have zero total momentum. When you let the air come out, it rushes out with high speed. It is pushed by the compressed air in the balloon, and it pushes back. It pushes back on that air, and that air pushes on the balloon. The released air goes one way, and the balloon containing its remaining air goes the other way, and the two momenta cancel.

When you sneeze, the sudden rush of air outward likewise can push your head backwards. In the opening of this chapter, there was a puzzle: how much does the astronauts head snap back. I read in a newspaper once that the head would snap back at a dangerous speed because the head was weightless in space. That's not true, of course. The writer of the article had confused weight with mass. The astronaut's head has no weight but it has every bit as much mass as it did on Earth. The force of the sneeze will accelerate the head backwards by an amount given by F = k m a, but since m is the same as on Earth, the acceleration a will be no greater.

Skyhook

Ponder the Space Shuttle. To put 1 kg payload into space requires 28 kg (fuel + container + rocket). Suppose, instead, we built a tower²⁷ that went all the way up to

²⁷ In the Bible, such a tower was attempted in ancient Babylon, and it is also referred to as the "Tower of Babylon." Its goal was to reach heaven. To prevent the Babylonians from succeeding, God made all the workers speak different languages. Thus, according

²⁶ The external tank hold 751 tons of fuel, and there are two solid rocket boosters that weigh 590 tons each, for a total of 1931 tons.

space. How much energy would it take to haul the kilogram up to the top, using an elevator? According to the section "Escape to Space", the energy required take a gram of material to infinity is 15 Calories. That's roughly the energy in 1.5 grams of gasoline (not including the oxygen). So if we had a tower with the elevator, ran the motor below (where it could use air) getting to space would take 28/1.5 = 19 times less fuel.

Many people have pondered the fuel waste from rockets. Although a tower to space seems impossible, it may make sense to hang a cable down from a geosynchronous satellite and use it to haul payload up, an idea once referred to as "project skyhook." The recent discovery of very strong carbon nanotubes has revived the idea. Arthur C. Clarke used this idea in his 1977 science fiction novel "Fountains of Paradise."

A more likely idea is to "fly" to space on an airplane. Airplanes have two attractive features: they use oxygen from the atmosphere as part of their fuel (so they don't have to carry it all, as do rockets) and they can push against the air, instead of having to push against their own exhaust. Although it is possible in principle, the technology to achieve 8 to 12 km/sec with airplanes does not yet exist. We'll talk more about airplanes in a moment.

Earlier in this chapter we mentioned the possibility of using "rail guns." These are long devices that achieve their high projectile velocities by using electric and magnetic forces to push on the projectile. But recall their limitation: they must be very long in order to avoid huge accelerations that could kill humans.

Ion rockets

The inefficiency of rockets comes from the fact that typical chemical fuels only have enough energy to give their atoms a velocity of 2-3 km per second. Rockets have been proposed that overcome this limitation by shooting out *ions*, a name for atoms that have an electric charge. You can find out a lot about these on the web. Like the rail gun, the ions can be given their high velocity through electric forces, so they are not limited to the 2-3 km/sec typical of rocket fuel. For example, a proton expelled at an energy of 100,000 eV has a velocity of 4400 km/sec. This makes ion rockets potentially much more efficient than chemical rockets, but so far nobody has figured out how to make the mass of the expelled ions sufficiently great to be able to launch a rocket from the Earth. They are more useful when a low thrust is needed for an extended period of time. NASA is planning on using ion propulsion on the upcoming Dawn Mission to the asteroids Vesta and Ceres (possibly launched as early as 2006).

to the Bible, is the origin of the multitude of languages spoken by humans. It is also the origin of the verb "to babble."

Flying: airplanes, helicopters, and fans

Airplanes fly by pushing air downwards.²⁸ Every second, the airplane tends to pick up downward velocity from the Earth's gravity. It stays at the same altitude by pushing enough air downward that it overcomes this velocity.

The fact that wings push air down is most readily observed in a "rotary wing" aircraft, otherwise known as a helicopter. (Helicopter pilots called the ordinary airplane a "fixed wing" aircraft.) In fact, the helicopter blades are designed to have a shape identical to wings, and air is pushed past them when they spin. They push the air down, and that is what pushes the helicopter upward. If you stand under a helicopter rotor when it is spinning, you can feel the air being forced downward.

It is probably more convenient, however, to observe how wing-shaped blades push air by standing in front of a fan. Fans work the same way as a helicopter blades, and as airplane wings. Movement through the air forces air perpendicular to the direction of motion of the blade.

For the airplane and the rocket, the v_R needed is the velocity to overcome the pull of gravity. In once second, gravity will give any object a velocity of

$$v = g t = 10 \text{ m/s}$$

This falling velocity must be cancelled by accelerating upward, and this is done in an airplane by pushing air downwards. Air is typically a thousand times less dense than the airplane (1.25 kg/m³), so to get enough air (i.e. to make the mass of the air large) the wings must deflect a large amount of air downward.

The wake of a large airplane consists of this downward flowing air, often in turbulent motion. It can be very dangerous for a second plane if it encounters this wake, since the amount of air flowing downward is large.

Flying: balloons

The first way that humans "flew" was in hot air balloons, in 1783 above Paris. These make use of the fact that hot air expands. It takes more volume compared to an equal

²⁸ In most physics books, the lift on the airplane wing is explained by use of a principle called Bernoulli's law. The "derivation" is done using a diagram that typically shows the air trailing the wing as if it is completely undisturbed. The astute student will be bothered by this. How can the air put a force on the wing but the wing not put a force on the air? A careful analysis (done in advanced aerodynamics books) shows that to establish a flow with higher velocity above the wing than below, the far field air velocity distribution is not undisturbed; it fact, it has air deflected downward with a momentum rate equal to the upward force on the wings, as it must to satisfy momentum conservation.

mass of cool air. Another way to say this is that the density of hot air (the mass per volume) is less than that of cool air.

In a liquid or gas, things that are less dense tend to float. That's why wood floats on water (if it has a density less than one gram per cubic centimeter; some woods sink). The heavier fluid "falls" and flows under the less dense object, pushing it upward. Boats float only if their average density (metal hull plus empty space inside) is less than that of water. That's why a boat will sink if it fills with water.

If you fill a balloon with hot air, it will rise until it reaches an altitude at which the density of the surrounding air matches that of the balloon. (Of course, you have to include the mass of the balloon, and any weight that it carries, along with the mass of the air inside.)

Better than hot air are light gases such as hydrogen and helium. Air weighs about 1.25 kg per cubic meter (at sea level). The same volume of hydrogen weighs about 14 times less, i.e. about 0.089 kg = 89 grams.²⁹ If we fill a one-cubic-meter balloon with hydrogen, it will tend to float. Calculate how much 1 cubic meter of air weighs, and how much one cubic meter of hydrogen weighs. The "lift" (upward force) of the balloon is just equal to the difference between these. Putting this into numbers, it means that a cubic meter balloon will have a lift of 1.25 - 0.089 = 1.16 kg. That means that if you hang an object from it that weighs less than one kilogram (including the mass of the balloon skin), it will still go upwards.

Helium gas isn't quite as light as hydrogen gas, so if the balloon is filled with helium, the lift isn't quite as much. Here's the calculation: helium gas weighs about 0.178 kg per cubic meter. So the lift on a helium balloon would be 1.25 - 0.178 = 1.07 kg. Note that even though the helium is twice as dense as hydrogen, the lift is almost as good.

But 1.16 kg of lift for a cubic meter of balloon is not really much. That's why, despite the cartoons you may have watched on TV, even a large packet of balloons are not enough to lift a 25 kg child. (If you have some spare time, and want to be amused, look up "Lawnchair Larry" on the internet.)

Hot air balloons have even less lift. If you heat the air to 300 C, then it's temperature in absolute scale is 600 K. That's twice its normal temperature, so its density is half of its usual density. The lift of a cubic meter would be 1.25 - 1.25/2 = 0.62 kg per cubic meter. Notice that that is significantly worse than hydrogen or helium. To lift a person who weighs 100 kg (including basket, balloon skin, cables) would take 100/0.62 = 161 cubic meters of hot air. If the balloon were shaped like a cube, the side of such a balloon would be $\sqrt[3]{161} = 5.4$ meters = 18 feet. That's why hot air balloons have to be so big, and why they don't lift much.

²⁹ Nitrogen has an atomic weight (number of neutrons plus protons) of 14. Hydrogen has an atomic weight of 1. The number of atoms in a cubic meter is the same for both gases, so the factor of 14 simply reflects the larger nitrogen nucleus.

Floating on water

The same principles apply to floating on water. Salt water is denser than fresh water, so the density difference between it and you is greater; that's why you float higher in salt water. Even strong swimmers take advantage of their buoyancy (the fact that they are less dense, on average, than water). If water becomes filled with bubbles, its average density can become less than yours, and you will sink. The New York Times on August 14, 2003, had an article describing how a group of boys drowned because they were in bubbly water.³⁰ Undersea volcanic eruptions have led to bubbly water in the oceans, and in such water even ships will sink.

Submarines can adjust their depth below the ocean surface by taking in and expelling water into their ballast tanks. When they take in water, the air in the tanks is replaced by the heavier water, and the average density of the submarine increases. This makes the submarine sink. The only thing that will stop the sinking is expulsion of water from the tanks. If the submarine sinks too far, then it is crushed by the weight of the water above it; that makes it even more dense, and so it sinks faster. That is called the hull crush depth. In the movie "Crimson Tide," that depth was 1800 feet, about 1/3 mile down. The submarine in that movie (the fictional USS Alabama) was able to save itself by getting its engine running, and using its short "wings" to get lift in way similar to the way that an airplane does, by moving forward and pushing water downward. A submarine can also push compressed air into its ballast tanks, driving out the water, and decreasing its average density.

To four teenagers from the suburbs, Split Rock Falls was a magical place — cool water rushing between the granite walls of a mountain ravine, forming pools for hours of lazy summertime swimming.

On Tuesday afternoon the four men — Adam Cohen, 19; Jonah Richman, 18; Jordan Satin, 19; and David Altschuler, 18 — returned to their favorite childhood summer haunt to find it engorged by a summer of heavy rain. By the end of the day, all four men, each an experienced swimmer, was dead, drowned in the waters they knew well.

In what officials here described as one of the worst drowning accidents ever in the Adirondack State Park, all four died after Mr. Altschuler slipped off a narrow granite ledge into a foaming pool of water whipped into a frenzy by a tumbling waterfall. In a final act of friendship, Mr. Richman, Mr. Cohen and Mr. Satin, who had grown up together on Long Island, jumped after him to try to save his life, police and officials said. The laws of physics were against them, though.

"They call it a drowning machine," said Lt. Fred J. Larow, a forest ranger with the State Department of Environmental Conservation, who helped recover the bodies here, about 20 miles east of Lake Placid. "The water was so turbulent and aerated that there was no way they could stay above water. Even the strongest swimmer in the world couldn't have survived it."

³⁰ Here is a quote from that article:

Sperm whales are said to be able to dive as deep at 2 miles. Diving deep is easy, since as the whale goes deeper, any air in its lungs (remember, a whale is a mammal) is compressed, and that makes the whale less buoyant. So once the whale is denser than water, it will sink. Coming up is the hard part. Whales save enough energy in their effortless dives, to be able to swim back up to the surface.

Air pressure on mountains, outside airplanes and satellites

Air pressure is simply the weight of the air above you. In any fluid or gas, the pressure is evenly distributed, so that the air at sea level will push an equal amount up, down, and sideways. As you go higher, there is less air above you, so the pressure decreases. At an altitude of 18,000 feet (3.4 miles, 5.5 km) the pressure is half of what it is at sea level. That is the altitude of Mt. Kilimanjaro in Africa, and many people walk to the top every year. They go above half the atmosphere! It is hard to breath up there, and nowhere on Earth do people live continuously at that altitude. But if you only spend a day or two going up and down, you can take it. Go up another 18,000 feet – to 36,000 feet, and the pressure is reduced by another factor of 2 – to one quarter the pressure at sea level. That's a typical altitude for jet airplanes. And that rule continues; for every additional 18000 feet, the pressure (and the density of the air³¹) drops by another factor of two. You can not live at such a low density of air, and that is why airplanes are pressurized. You can live at that pressure if the "air" you are given is pure oxygen (rather than 20%), and that is what you would get from the emergency face masks that drop down in airline seats if the cabin ever loses pressure.

Want to know the decrease in air pressure? Divide the altitude by 18000 ft (or by 5.5 km, if that's how you've measured it). The number you get is the number of halves you have to use. Suppose your altitude (e.g. in an airplane) is 40,000 ft. Divide that by 18000 to get about 2 halvings. That means the pressure is reduced by a factor of (1/2)x(1/2) = 1/4. So the pressure (and the air density) is 4 times less than at sea level.

Now consider a "low earth orbit" satellite, at H = 200 km above sea level. Let's do all our calculations in kilometers. So we use the half altitude distance to be 5.5 km. Then $H/5.5 = 200/5.5 \approx 36$. Now multiply (1/2) by itself 36 times to give:

$$P = (1/2)^{36} = 1.45 \text{ x} 10^{-11} = 0.00000000001$$

That's a pressure of 10 trillionths times as small as at sea level.³² Satellites need this low pressure to avoid being slowed down by collisions with air. A typical altitude for a LEO (remember? "Low Earth Orbit") is 200 km.

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³¹ The air density doesn't drop quite that much because the air up there is cooler.

³² The equation implicitly assumed that the temperature of the air continues to cool at higher and higher altitude. But above the tropopause the temperature rises, and that makes this calculation interesting, but not really accurate.

Because the density of air decreases with altitude, a helium balloon will not rise forever. Eventually it reaches an altitude at which the outside air has the same density as the helium (with the weight of the gondola averaged in), and then it stops rising. I noticed this as a child, when I was disappointed to see that the helium-filled balloon I had released did not go all the way to space, but went high up and then stopped rising. That's why balloons are not a possible way to get to space.

Space – and the X Prize

How high do you have to go to reach space? That depends on your definition. You never get far enough to completely escape the Earth's gravity, and likewise, there no matter how high you get, there will always be some atmosphere (even if only one molecule per cubic mile). Since the lowest satellite will fly, at least for a few orbits, if it orbits at an altitude of 100 km, some people have defined this altitude as being "space". (Even at 100 km there is enough atmosphere to bring slow the satellite after a few orbits, and bring it to the surface.)

To encourage private companies to set rockets or aircraft into space, a private foundation created the "X Prize" for the first private organization to send a human to that altitude. I'm not going to go into all the details of this prize, because it is far less interesting than most people think. There is a huge difference between reaching 100 km altitude, and orbiting the Earth. Way back in 1946 the US government launched a modified German V-2 rocket to an altitude of 187 km – but it was not until 1957, eleven years later, that the Soviet Uniion launched the first Earth orbiting satellite.

It is much harder to put a satellite into orbit, than to just get up 100 km. To get a feel for this, imagine that there is NO atmosphere on the Earth. Suppose we want to shoot a bullet straight up, and have it reach an altitude of 100 km. How fast must it leave the gun? The answer is 1.4 km/sec. For students who have studied the equations, I put the calculation in the footnote.³³ Compare this to the speed needed for orbit: 8 km/sec. Orbital speed is 5.7 times greater than the speed it takes to get up 100 km. Moreover, the kinetic energy depends on the square of the velocity, so the energy needed is (5.7)² bigger, a factor of 33. So it takes 33 times as much energy to get into orbit than to merely reach 100 km altitude.

So why is there so much excitement over the X Prize? I think it is because very few people know about this factor of 33. The winners of the X Prize certainly understand, but they don't want to publicize that. The \$10 million prize was not enough to cover their expenses! So how will they make money? Not by sending up satellites. They can't

for v gives v = sqrt(2E6) = 1414 m/sec = 1.4 km/sec.

-30-

³³ Optional: speed to reach 100 km. The energy to reach height h is E = mgh, where g is the acceleration of gravity, approximately equal to 10 meters/sec every second. For m = 1 km, and h = 100 km = 1E5 meters, this is E = 1 x 10 x 1E5 = 1E6 joules. The velocity that you have to give that mass can be calculated from E = $\frac{1}{2}$ m v² = 1E6 joules. Sovling

accomplish that any more than the US could with the V-2 rocket. The interesting answer: the winners of the X Prize will earn money by getting tourists to fly up 100 km, and then telling the tourists that they now qualify as "astronauts".

Convection – thunderstorms and heaters

When air is heated near the ground, its density is reduced, and it tends to rise, just like a hot air balloon. Unconstrained by any balloon, the air expands as it rises, and an interesting result is that it will remain less dense than the surrounding air until it reaches the "tropopause", the level in which ozone absorbs sunlight causing the surrounding air to be warmer. When it reaches the tropopause, its density is no longer less than that of the surrounding air, so the air stops rising.

On a summer day, when thunderstorms are growing, it is easy to spot the tropopause. It is the altitude at which the thunderstorms stop rising, and begin to spread out laterally. The tropopause is a very important layer in the atmosphere. It is the location of the "ozone layer" which protects us from cancer-producing ultraviolet light. We'll talk more about his layer in Chapter 8 Waves (because of the important effect it has on sound), and in Chapter 10 Invisible light, when we discuss ultraviolet radiation and its effects.

Convection is the name we give to the process of hot air expanding and rising. When you have a heater in a room near the floor, the rising hot air forces other air out of the way; that results in a circulation of the air. This is a very effective way to warm a room – much faster than heat conduction through the air. But it invariably results in the warmest air being near the top of the room. If you put the heater near the top, the warm air just stays up there. On a cold day, in a room with a heater near the floor, stand up on a stepladder and feel how much hotter it is near the ceiling.

Optional: Angular momentum and torque

In addition to ordinary momentum (mass times velocity), there is another kind of momentum that physicists and engineers find enormously useful in their calculations called angular momentum. Angular momentum is similar to ordinary momentum but it most useful for motion that is circular, i.e. rotation. If an object of mass M is spinning in a circle of radius R, moving at velocity v, then its angular momentum L is:

$$L = M v R$$

What makes angular momentum so useful is that, like ordinary momentum, when there are no external forces on an object, it is "conserved", i.e. its value doesn't change. Have you ever spun on ice-skates? Actually, ice skates are not necessary – just stand in a spot and start spinning with your arms stretched out. If you've never done this, then I strongly recommend you try it right now. Then rapidly pull your arms in. (You'll never forget the experience, and you can have great fun entertaining children with it.) To the surprise of

most people, they will suddenly spin much faster. You can predict that from the angular momentum equation. If the angular momentum L is the same before and after the arms are pulled in, and the mass of the arms M is the same, then v R must be the same. If R gets smaller, then v must get bigger.

Angular momentum conservations also explains why water leaving a tub through a narrow drain begins to spin. In fact, it is very unlikely that the water in the tub wasn't already spinning, at least a little bit. But when the distance to the drain (R, in the equation) gets small, the v in the equation gets very big. A similar effect occurs in hurricanes and tornadoes. Air being sucked into the center (where there is a low pressure due to air moving upward) spins faster and faster, and that's what gives the high velocities of the air in these storms. The air in hurricanes gets its initial spin from the spin of the Earth, and then they amplify it by the angular momentum effect. So hurricanes really do spin in different directions in the Southern and Northern Hemispheres.

It is not true that sinks or tubs drain differently in the northern and southern hemispheres. Their direction depends on the small residual rotation in the water left over from the filling of the tub, or from a person getting out.

Conservation of angular momentum can be used to understand how a cat, dropped from an upside down position, can still land on his feet. (Don't try this one at home! I never have, but I've seen a movie...) If he spins his legs in a circle, his body will move in the opposite direction, keeping his total angular momentum equal to zero. That way he can bring its legs underneath him. Astronauts do this trick when they want to reorient themselves in space. Spin an arm in a circle, and your body will move in the opposite direction. You can try that trick on ice skates too.

The conservation of angular momentum has other useful applications. It helps keep a bicycle wheel from falling over, when the wheel is spinning. It can also cause a difficulty: if kinetic energy is stored in a spinning wheel (usually called a "flywheel"), then the angular momentum makes it difficult to change the direction that the wheel is spinning. This makes its use for energy storage in moving vehicles, such as buses, problematical. It is often addressed by having two flywheels spinning in opposite directions, so although energy is stored, the total angular momentum is zero.

Angular momentum can be changed by a suitable application of an outside force. The required geometry is that the force must act obliquely, at a distance. We define torque as the tangential component of the force (the oblique part) times the distance to the center. So, for example, to start a bicycle wheel spinning, you can't just push on the rim in a radial manner. You have to push tangentially. That's called torque. The law relating torque and angular momentum is this: the rate of change of angular momentum is numerically equal to the torque.

You can probably see why mastery of the equations of angular momentum is very useful to engineers and physicists in simplifying their calculations.

END OF CHAPTER

Quick review

Weight is the force of gravity acting on your mass. The force of gravity is an inverse square law, so when the distance increases by (for example) 3, the force becomes 9 times weaker. It is this force that keeps the Moon in orbit around the Earth, and the Earth in orbit around the Sun. If gravity were turned off, satellites would move in straight lines rather than in circles. Even at great distances, the force of gravity never goes completely to zero. The sensation of weightlessness felt by astronauts is really the sensation of continuous falling.

All satellites must keep moving, or they fall to Earth; they cannot hover. In LEO, the satellite moves at 8 km/sec, and orbits the Earth in 1.5 hours. LEO satellites are useful for Earth observations, including spying. Geosynchronous satellites are useful for applications where the position of the satellite must stay fixed with respect to the ground. A medium Earth orbit (MEO) is in between. GPS satellites are MEO. A GPS receiver determines its location by measuring the distance to three or more of these satellites.

Close to the Earth (where we live) objects fall with constant acceleration, i.e. their velocity v = g t, until they are slowed down by air resistance. The distance they fall is $h = (1/2) g t^2$. Air resistance increases with the square of the velocity. If you go 3 times faster, the force of air resistance gets 9 times larger. Air resistance limits the velocity of fall to no more than the "terminal velocity." This depends on the area and mass of the object, and is different for people (60-100 mph), parachutes (15 mph), and large objects such as King Kong. Air resistance also limits the fuel efficiency of automobiles. Satellites must fly high (> 200 km) to avoid air resistance.

A force on an object makes it accelerate by an amount (given in m/s per sec) of F = k m a

This is known as "Newton's Second Law." (k = 0.224 is a constant that makes the units come out in pounds.) Acceleration can also be measured in units of g, the acceleration of gravity. The g-rule says that to accelerate an object to 10 g requires a force 10 times as great as that object's weight. That's about the limit for a human to endure, so higher accelerations (e.g. the rail gun) can't be used. The Space Shuttle never accelerates more than 3 g. Circular motion can also be considered to be acceleration, with Newton's Second Law applying, even if the magnitude of the speed doesn't change. Based on this, we can calculate the velocity a satellite must have to stay in a circular orbit at different altitudes above the Earth.

The surface gravity on other planets and on asteroids is very different than it is on the Earth, science fiction movies notwithstanding.

To escape to space completely requires an energy of about 15 Calories per gram. This is enough energy to lift you up a big enough elevator, if one could be built ("skyhook"). If you have a velocity of 11.2 km/sec, then your kinetic energy is sufficient to escape. Black holes are objects whose escape velocity exceeds the speed of light.

Gravity measurements have practical applications. Since oil is lighter than rock, it has a weaker gravity, and that fact has been used to locate it. Gravity measurements give us the best image of the Chicxulub crater.

When a gun is fired, the bullet goes forward and the gun goes backward. This is an example of the conservation of momentum. Other examples: Rockets go forward (very inefficiently) by shooting burnt fuel backwards. Airplanes and helicopters fly by pushing air downwards.

Objects float when their density is less than that of the fluid or gas they are in. That includes boats and balloons. Hot air rises because it is less dense than the surrounding air, and that happens for hot air balloons and thunderstorms. The density and pressure of air decreases with altitude according to a halving rule:

$$P = (1/2)^{H/6.9}$$

where the height H is expressed in km.

Angular momentum (a momentum that applies to circular motion) is also conserved, and that causes contracting objects to speed up. Examples include sink drains, hurricanes, and tornadoes.

Qualitative questions
At high velocities, most of the fuel used in an automobile is used to overcome () gravity () momentum () air resistance () buoyancy
Airplanes fly by () pushing fuel downward () pushing fuel backwards () pushing fuel upwards () pushing air downwards
At an altitude of 200 km, the downward force of gravity on an Earth satellite is () the same as on the surface of the Earth () a little bit weaker () zero () a little bit stronger
In the southern hemisphere, sinks drain () usually clockwise () the same way they do in the Northern Hemisphere () the answer is different in the Eastern and Western Hemispheres.
A rail gun () accelerates rails

() can shoot bullets faster than ordinary guns

() doesn't really accelerate things () uses ions for propulsion
The Sun would be a black hole if it were squeezed into a radius of () 2 miles () 2,000 miles () 2 million miles () It already is a black hole
The method that would take the least energy to get something to space is: () lift it by elevator (if the elevator existed) () launch it in a one-stage rocket () fly it in a balloon () launch it in a three-stage rocket
If an artificial satellite orbited the Earth at the distance of 240,000 miles (the present distance to the moon), it would orbit the Earth in a period of () 90 minutes () 1 day () 1 week () 1 month
The time it takes a geosynchronous satellite to orbit the Earth is: () 90 minutes () 1 day () 1 week () 1 month
A typical terminal velocity for a high diver is closest to: () 1 mph () 10 mph () 100 mph () 1000 mph
The force of gravity between two people standing next to each other is () zero () too small to measure () small but measurable () greater than 1 kg
For a low Earth satellite (altitude 200 km), the force of gravity is () zero () a few percent less than on the Earth's surface () exactly what it is on the Earth's surface () about half of what it is on the Earth's surface

The altitude of a geosynchronous satellite is closest to: () 200 miles () 26,000 miles () 2,000,000 miles () 93,000,000 miles
Rockets fly by () using antigravity () pushing air downwards () pushing fuel downwards
() being lighter than air
Balloons rise until () the surrounding air becomes too dense () the surrounding air becomes too thin (not dense) () the surrounding air becomes too cold () they reach space
You can see where the tropopause is by
() looking at Earth satellites() seeing how high birds fly
() looking at the tops of thunderstorms
() seeing where lightning comes from
Ice skaters spin faster by pulling in their arms. This illustrates that
() momentum is conserved() angular momentum is conserved
() energy is conserved
() angular energy is conserved Someone firing a rifle is pushed back by the rifle. This illustrates that
() momentum is conserved
() angular momentum is conserved
() energy is conserved() angular energy is conserved
() angular energy to combet to
Internet research topics
See what you can find on the internet about the following topics:

Manufacturing objects in space
Project skyhook
Spy satellites
Rail guns

Black holes
Ion propulsion
GPS
Lawnchair Larry
Ion engine

Essay questions

Automobiles and trucks are often designed with a tapered ("aerodynamic") rather than a blunt front surface. Why is this? What does the tapered front accomplish? How important is it?

Artificial Earth satellites fly at different altitudes, depending on what they need to do. Describe the differences between low Earth satellites, medium Earth satellites, and geosynchronous satellites. For which applications would you use each?

Which would fall faster, a high diver doing a "swan dive" (in which he spreads out his arms and falls chest-first) or a diver with his arms pointed above his head going straight down? Why? Explain the relevant physics.

When the diver enters the water, having your head down is much less painful than a "belly-flop." Discuss this in terms of the "area" that hits the water.

Science fiction movies and action movies often show things that don't fit in easily with the laws of physics. Give examples. Can you think of additional examples not described in this text book?

Black holes: Why can't we see them? How do we know they are there? Are any known to exist?